CLAIMS

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- 1. A method of performing modular multiplication of integers X and Y to produce a result R, where R = X.Y mod N, in a multiplication engine, comprising the steps of:
- (a) fragmenting X into a first plurality of words x_n each having a first predetermined number of bits, k;
- (b) fragmenting Y into a second plurality of words y_n each having a second predetermined number of bits, m;
- (c) pre-calculating multiples of a word x_n of X in a pre-calculation circuit and using said pre-calculated multiples to derive products of the word x_n of X with each of the plurality of words y_n of Y;
 - (d) computing an intermediate result R_j as a cumulating sum derived from said pre-calculated multiples;
- 15 (e) for each successive word of X, repeating the steps of pre-calculating and computing so as to generate successive intermediate results, R_j , for each of the first plurality of words x_n ; and
 - (f) providing as output each of the intermediate results R_j so as to form a final result.
 - 2. The method of claim 1 in which X is fragmented into n words of k bits each, according to the expression $X = x_{n-1}B_x^{n-1} + x_{n-2}B_x^{n-2} + ... + x_0$, where $B_x = 2^k$.
 - 3. The method of claim 1 in which Y is fragmented into n words of m bits each, according to the expression $Y = y_{n-1}B_y^{n-1} + y_{n-2}B_y^{n-2} + ... + y_0$, where $B_y = 2^m$.
- 4. The method of claim 1 in which the step of computing an intermediate result R_j comprises generating a succession of terms x.y + c + z for addition, comprising the steps of:

- (i) reading a pre-calculated multiple of a word x_n of X to form an $x_n.y_n$ product,
- (ii) adding a carry word ci. from a previous term;
- (iii) adding a corresponding term, z, from a previous intermediate result;
- 5 (iv) fragmenting the result into a lower order m-bit word and a higher order, k-bit carry word;
 - (v) repeating steps (i) to (iv) for each of the x_n . y_n products; and
 - (vi) after use of all $x_n.y_n$ products, forming a final term by adding the final carry word and corresponding term from the previous intermediate result.

5. The method of claim 4 wherein the step of computing the intermediate result is implemented as:

$$R_{j} = x_{n-j+1}y_{0} + (x_{n-j+1}y_{1} + r_{j-1,0})B_{y} + (x_{n-j+1}y_{2} + r_{j-1,1})B_{y}^{2} + \dots + (x_{n-1}y_{n-1} + r_{j-1,n-2})B_{y}^{n-1} + r_{j-1,n-1})B_{y}^{n}$$

6. The method of claim 1 in which step (f) further includes combining all the intermediate results R_{j} to form R, according to the expression

$$R = ((((x_{n-1}Y \mod N)B_x + x_{n-2}Y) \mod N)B_x + ...x_0Y) \mod N.$$

- 7. The method of claim 4 in which step (i) comprises the steps of reading selected basic multiples of the word x_n of X and combining them to obtain the product $x_n.y_n$.
- 8. The method of claim 7 in which steps (i), (ii) and (iii) include combining the selected basic multiples of the word of X, the carry word c_j , and the corresponding term z in an adder circuit (70).

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- 9. The method of claim 4 in which the corresponding term z from a previous intermediate result is the immediate less significant word from the previous intermediate result.
- 5 10. The method of claim 4 in which the corresponding term z from a previous intermediate result is a (k/m)th less significant word from the previous intermediate result.
- 11. The method of claim 1 in which the steps of pre-calculating comprise the steps of:

calculating pre-selected basic multiples of the word of X and combining selected ones of the basic multiples to form a desired x.y product.

- 12. The method of claim 4 in which the pre-calculation of multiples of a word of X takes place during step (vi) for the previous word.
 - 13. Apparatus for performing modular multiplication of integers X and Y to produce a result R, where R = X.Y mod N, comprising:

means for fragmenting X into a first plurality of words x_n each having a first predetermined number of bits, k;

means for fragmenting Y into a second plurality of words y_n each having a second predetermined number of bits, m;

a pre-calculation circuit (10) for pre-calculating multiples of a word x_n of X and using said pre-calculated multiples to derive products of the word x_n of X with each of the plurality of words y_n of Y;

means for computing an intermediate result R_j as a cumulating sum derived from said pre-calculated multiples; and

control means for controlling repetition of the pre-calculations and computing of an intermediate result for each successive word of X so as to generate successive intermediate results, $R_{\rm J}$, for each of the first plurality of words $x_{\rm n}$.

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- 14. The apparatus of claim 13 in which the means for computing an intermediate result R_j generates a succession of terms x.y + c + z for addition, including:
- (i) means (60) for reading a pre-calculated multiple of a word x of X to form an x.y product,
- (ii) means (70) for adding a carry word c_j, from a previous term;
- (iii) means (70) for adding a corresponding term, z, from a previous intermediate result;
- (iv) means for fragmenting the result into a lower order m-bit word and a higher order, k-bit carry word;
- (v) control means for effecting repetition of the reading of a precalculated multiple and addition of the carry word and corresponding term for each of the x.y products and forming a final term by adding the final carry word and corresponding term from the previous intermediate result.

15. A calculation circuit (10) for providing each of a plurality of multiples of an integer x, to form products x.y, comprising:

adder and shift circuits (30, 50) for deriving a plurality of basic multiples of x;

a plurality of registers (20) for storing at least some of said plurality of basic multiples of x;

a plurality of multiplexers (60, 160) each receiving said basic multiples of x, each multiplexer having selection lines (Y) for receiving selected bits of a selected y word; and

- a summation circuit (70, 161...181) for receiving the outputs from each multiplexer and combining them according to the numeric significance of the portion of the y word used as input to the respective multiplexer selection line.
- 30 16. The calculation circuit of claim 15 in which the plurality of registers (20) correspond to selected odd basic multiples of x, even basic

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multiples of x being provided to each multiplexer by bit shifting lines (50) coupled to selected ones of the plurality of registers.

17. The calculation circuit of claim 15 in which:

the plurality of multiplexers comprises a set of logic gates (161...167) each having a first input (x_i) connected to receive a respective basic multiple of x, and a selection line (S_i) to enable assertion of the basic multiple at an output thereof, and

the summation circuit comprises a series of adders (161...181) for receiving all asserted outputs of the series of logic gates,

wherein only logic gates in the set of logic gates for which a selection input has changed will be switched during a change in the selected y word.

- 18. A computer program product, comprising a computer readable medium having thereon computer program code means adapted, when said program is loaded onto a computer, to make the computer execute the procedure of any one of claims 1 to 12.
- 19. A computer program, distributable by electronic data transmission, comprising computer program code means adapted, when said program is loaded onto a computer, to make the computer execute the procedure of any one of claims 1 to 12.